BLUE: A Bipedal Robot with Variable Stiffness and Damping

Alexander Enoch*, Andrius Sutas*, Shin’ichiro Nakaoka†* and Sethu Vijayakumar*
*Institute of Perception, Action and Behaviour, School of Informatics, University of Edinburgh, United Kingdom
†Intelligent Systems Research Institute, National Institute of Advanced Industrial Science and Technology (AIST), Japan
E-mail: [a.m.enoch@sms., a.sutas@sms., sethu.vijayakumar@jed.ac.uk, s.nakaoka@aist.go.jp

Abstract—Exploiting variable impedance for dynamic tasks such as walking is both challenging and topical – research progress in this area impacts not only autonomous, bipedal mobility but also prosthetics and exoskeletons. In this work, we present the design, construction and preliminary testing of a planar bipedal robot with joints capable of physically varying both their stiffness and damping independently – the first of its kind. A wide variety of candidate variable stiffness and damping actuator designs are investigated. Informed by human biophysics and locomotion studies, we design an appropriate (heterogenous) impedance modulation mechanism that fits the necessary torque and stiffness range and rate requirements at each joint while ensuring the right form factor. In addition to hip, knee and ankle, the constructed robot is also equipped with a three part compliant foot modelled on human morphology. We describe in detail the hardware construction and the communication and control interfaces. We also present a full physics based dynamic simulation which matches the hardware closely. Finally, we test impedance modulation response characteristics and a basic walking gait realised through a simple movement controller, both in simulation and on the real hardware.

I. INTRODUCTION

A key motivator for the development of variable impedance actuators is to create robots which are inherently more robust to disturbances, more energy efficient, or more human-like. A problem which combines all of these is bipedal locomotion, and it is that problem that we start to tackle in this work, by producing a bipedal robot capable of varying both the stiffness and damping of its joints independently. Human mobility is dominated by walking: our actuation is provided by complex antagonistic arrangements of muscle tendon complexes, each of which exhibits a non-linear compliant behaviour [1], i.e., the compliance is built into our dynamics. By co-contraction of pairs of muscles, we can alter the stiffness of a joint, tensing up when appropriate to deal with the environmental uncertainties and task demands. Such co-contraction also changes the damping of the joint [2]. We deal with walking as a dynamic periodic process, a controlled fall that is typically modelled as a bouncing gait [3].

Robotics has yet to match the ease, energy efficiency, and robustness of human walking. Traditional bipedal robots with rigid joints (e.g. [4], [5]) are energetically inefficient, and not inherently robust to disturbances in terrain. Passive dynamic walkers (e.g. [6]) are incredibly energy efficient, but cannot perform any tasks other than walking at the speed they were designed for. Torque controlled bipedal robots allow simulation of compliance [7] [8], but without any of the physical advantages that passive compliance provides.

Very few bipedal robots capable of varying joint impedance have been designed. Some have antagonistic non-linear springs [9] or pneumatic muscles [10]; however, these have tended to be slow and not capable of exhibiting dynamic effects. A more agile, antagonistic pneumatic robot is described in [11], but compliance control of its joints is still fairly primitive. Veronica [12] (see also [13], [14]), built around MACCEPA variable stiffness joints, is only capable of achieving relatively low joint stiffness. MABEL [15], a planar biped, uses unidirectional leaf springs to give bounce to its legs, and has used these to store energy during locomotion. However, it is not capable of varying the stiffness of its individual joints and does not have ankle joints or feet.

We therefore aim to develop a bipedal robotic platform which combines the functional flexibility of traditional rigid joint robots with the energy efficiency and robustness to disturbances of passive dynamic walkers. The brief includes a robot that should have fine control over its stiffness and damping, hence, providing a unique platform for research into the effects of physically varying these parameters during...
walking and other movements.

By looking at human locomotion studies (e.g. [16]), we see that there is a significant amount of "negative work" done during the gait cycle, that is to say, work which is done on the body from external forces. Table I shows a summary of joint power over a gait cycle at a self selected preferred walking speed. Note that, especially in the knee and ankle, there is a significant amount of negative work done, and we try to design a robot which is capable of storing some of this in order to reduce the amount of positive work required from the motors. In the knee we see that damping would be especially useful for dissipating energy without requiring work from the drive motors.

In order to create a robot with interesting dynamic effects, but one which is not so bulky as to be difficult to manoeuvre in the lab, we define the hip rotation height to be 700mm and the target weight to be 25kg. This makes the robot around \( \frac{2}{3} \) of the size of the average American soldier [17]. All of the robot’s links are scaled from this anthropometric data.

In this paper, we introduce the planar bipedal robot BLUE (Bipedal Locomotion at the University of Edinburgh). We first study the available mechanisms for variable stiffness and variable damping, and select those which seem best suited to actuating a large dynamic walker. The robot itself is then designed around these mechanisms, with powered hip, knee and ankle joints, and a three part compliant foot. We show data from simulations of the platform, and finally show experimental validation of the designed platform and some basic initial movement controllers.

II. CHOOSING MECHANISMS FOR VARIABLE STIFFNESS AND DAMPING

Joints with variable stiffness or damping are far more complex than a traditional rigid robot joint, and the choice of these mechanisms will have a large bearing on the design of the robot as a whole. Therefore as the starting point for our design we look at the field of variable impedance, to see which types of mechanisms would be most suitable for the task at hand. There have been a great many designs published recently for variable stiffness mechanisms. Fewer have been published for variable damping.

A. Variable Stiffness Mechanisms

Variable stiffness designs can be broken down into three major categories: antagonistic, series pretension, and tunable springs.

<table>
<thead>
<tr>
<th>Power (W kg(^{-1}))</th>
<th>Summed Positive: 0.72 ± 0.13</th>
<th>Summed Negative: 0.37 ± 0.06</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hip Positive: 0.28 ± 0.07</td>
<td>Hip Negative: 0.03 ± 0.03</td>
<td></td>
</tr>
<tr>
<td>Knee Positive: 0.12 ± 0.06</td>
<td>Knee Negative: 0.20 ± 0.06</td>
<td></td>
</tr>
<tr>
<td>Ankle Positive: 0.32 ± 0.08</td>
<td>Ankle Negative: 0.14 ± 0.04</td>
<td></td>
</tr>
</tbody>
</table>

TABLE I
AVERAGE MECHANICAL POWER OVER FULL GAIT CYCLE IN HUMAN WALKING FROM UMBERGER 2007 [16]

1) Antagonistic: Antagonistic designs typically have two actuators pulling through springs in series, and alter stiffness by co-contracting these springs. It can easily be shown that for co-contraction to change stiffness, non-linear springs must be used, and so most designs for antagonistic variable stiffness focus on creating a suitable non-linear spring (e.g. [18] [11] [19]) or arranging linear springs in such a way as to create non-linearity [20].

Antagonistic designs increase stiffness by co-contracting, this uses a significant amount of energy and implies that some of the energy storage potential of the springs is wasted. Keeping such a joint stiff also involves expending energy, unless the actuators used are non-backdriveable. Furthermore, two powerful actuators are required, unless the compliant elements are bidirectional, or a more complex design is used [21] [22].

2) Series Pretension: Series pretension devices have a spring in series with the actuator, with a design such that the spring can be pre-stressed in order to increase joint stiffness [12] [23] [14]. These mechanisms also share the problem that changing stiffness wastes energy and means that the full energy storage potential of the actuator is not available at all stiffness settings.

3) Tunable Springs: Tunable spring designs rely on changing the geometry of a compliant element in series with an actuator in order to adjust the stiffness (e.g. [24] [25] [26]). Typically these mechanisms may have a smaller compliant range than other designs, but require little energy to change stiffness.

4) The MAwAS Variable Stiffness Mechanism: To get an idea of design requirements for locomotion, we look at typical walking data from human studies, which is normalised by leg length and body mass. We can see that we will need to generate output torques in the region of 30Nm, and whilst the exact amount of compliant deflection required will depend on control strategy, it is generally desirable to have this maximised (certainly larger than 20°). We also look at the negative work done on the joints to set a criteria for the minimum amount of energy storage required - for the ankle, this would amount to roughly 3.5J.

Considering these criteria, as well as the merits and demerits of the various types of variable stiffness mechanisms, we opted to utilise a modified version of the AwAS actuator [24], which we term the Modified AwAS (MAwAS). Our modifications have resulted in increased compliant range and also prevents uneven spring compression. We also use wave springs in order to make the design more compact.

Key advantages of this variable stiffness mechanism are:
- Ability to deliver torques > 30 Nm.
- Energy storage > 3.5J
- Reach low stiffness (to make use of passive dynamics)
- Good range of compliances
- Minimal energy required to change stiffness
- Holding joint at high stiffness requires no energy
- Simple to manufacture
- Energy storage independent of stiffness setting
• Stiffness ranges easily changed by swapping springs
• Becomes a rigid joint when compliant range exceeded, without any damage to springs

5) MAwAS joint dynamics: A schematic of the variable stiffness design is shown in Fig. 2. The joint drive motor on the input link moves an intermediate arm, shown in diagram in blue. This is connected via two compression springs to the output link, shown in grey. A second, smaller, motor is used to adjust the distance of the springs from the axis of rotation (r) by driving lead screws. As r increases, the amount of compression of the relevant spring for a given deflection from equilibrium (θ) increases, and thus so does the effective joint stiffness.

Calculating the torque and stiffness functions of the transmission as a function of r and θ is quite straightforward. The springs used are compression only, and thus, when the transmission is out of equilibrium by angle θ the compression of the spring, x, is given by x = rsinθ. The spring force F_s can then be computed as

\[ F_s = r K_s \sin \theta \]  
(1)

where \( K_s \) is the spring constant. The torque acting on the output link can thus be calculated by taking the component of the spring force which acts perpendicular to the output arm:

\[ T = \frac{r^2 K_s \sin(2\theta)}{2} \]  
(2)

We define the stiffness to be the derivative of the torque function with respect to θ, and this is given by:

\[ K = \frac{dT}{d\theta} = r^2 K_s \cos(2\theta). \]  
(3)

When the maximum compression of the spring is reached, the transmission hits a hard stop, and effectively becomes a rigid joint. The maximum deflection required to reach this rigid limit is given by:

\[ \theta_{\text{max}} = \sin^{-1} \left( \frac{l_{\text{comp}}}{r} \right) \]  
(4)

where \( l_{\text{comp}} \) is the maximum compression of the spring. With the size and target weight of the robot known, we look at studies of human walking kinetics (e.g. [16]) in order to compare likely required torques with compliant deflections – this aids in the selection of springs for the joints. It should be noted that it is a relatively trivial matter to change the springs in the variable stiffness mechanism in order to change the overall stiffness/deflection characteristics of the joint. For the hip joints, we use springs with \( K_s = 94540\text{N/m}, l_{\text{comp}} = 6.15\text{mm} \). For the knees and ankles we use springs with \( K_s = 29760\text{N/m}, l_{\text{comp}} = 19.66\text{mm} \).

Fig. 3 shows the torque and stiffness curves for the variable stiffness mechanism in both of the hips of the robot. Similarly, Fig. 4 shows these for the knees and ankles. Each graph also shows the maximum expected joint torque for walking as a dashed line, and uses the required energy storage and torque during an instant in the walking cycle to illustrate a point which will meet these criteria. It is necessary to choose springs which roughly meet the energy storage criteria, but also can be stiff enough to provide high torque for movements not just limited to walking.

6) Energy Storage in the MAwAS: The energy stored in the compliant transmission can easily be shown to be \( U_c = \)
The deflection from equilibrium is shown as a function of output torque and stiffness setting in Fig. 5(a), and the resulting energy stored in Fig. 5(b). These graphs are for the springs used in the knee and ankle joints.

7) Energy Cost of Changing Stiffness: A key concern in the choice of a mechanism for variable stiffness is the energy cost of changing stiffness. Since the MAwAS mechanism does not rely on pretension in order to change compliance, the energy used to change the stiffness setting is quite small. We consider the energy required to increase stiffness when the joint is out of equilibrium, keeping the energy stored in the system the same. In order to move the spring carriage and increase stiffness the component of spring force acting down the output link must be considered, this is given by $F_p = F_s \sin \theta$. Using eq. (1) it follows that:

$$F_p = \frac{F_s^2}{r K_s}$$

(5)

The energy used working against this force to change stiffness can therefore be calculated by a simple integration:

$$E = \int_{r_1}^{r_2} F_p dr$$

$$= \frac{F_s^2}{K_s} \left( \ln(r_2) - \ln(r_1) \right)$$

(6)

(7)

Using realistic numbers from our implementation, the total energy required to move from $r_1 = 0.0325$ to $r_2 = 0.078$ against a spring force of $F_s = 300$N, with a spring constant $K_s = 29760$N/m would use around 2.6J of energy. With lead screw transmission efficiency of 44% the energy used by the stiffness adjustment actuator should be around 6J. This is a very simplified calculation which does not include additional frictional forces, and assumes that the spring carriage itself is massless. Nevertheless, the power required to adjust the stiffness is very small compared to the power required to drive the joints.

B. Variable Damping Mechanisms

There have not been as many designs published for mechanisms to achieve variable damping. Some utilise Magneto-
Defining $\dot{\theta} = q - q_m$ as the deflection from equilibrium and using eq. (3), this can be rewritten as:

$$\ddot{\theta} + \frac{d}{J} \dot{\theta} + \frac{r^2 K_s}{J} \cos(2\theta) \dot{\theta} = -q_m - \frac{d}{J} \dot{q}_m$$  \hspace{1cm} (10)

For small oscillations around $\theta = 0$, $\cos(2\theta) \approx 1$. Therefore, the above dynamics can be simplified as

$$\ddot{\theta} + 2\zeta\omega_n \dot{\theta} + \omega_n^2 \theta = -q_m - 2\zeta\omega_n \dot{q}_m$$  \hspace{1cm} (11)

where $\omega_n = \sqrt{\frac{r^2 K_s}{J}}$ is the natural frequency and $\zeta = \frac{d}{2\sqrt{r^2 K_s}}$ is the damping ratio. Thus, by changing $r$ and $d$, we can change the natural frequency and damping behaviour of the joint.

In a more general sense, the equation of motion for the entire robot can be seen to be:

$$M(q) \ddot{q} + C(q, \dot{q}) \dot{q} + g(q) = T(\theta) + D \dot{q} + F_{ext}(q, \dot{q}, \ddot{q})$$  \hspace{1cm} (12)

where $M$ is the inertia matrix, $C$ represents Coriolis forces, $g$ introduces forces from gravity, $T$ is the torque from the variable stiffness transmission ($T_i = \frac{r^2 K_s}{J} \sin(2\theta_i)$). $D$ represents the variable damping, and $F_{ext}$ includes external forces, for e.g., due to ground contact forces.

### IV. Design and Construction of BLUE

BLUE has been built and initial testing completed. So far, the major joints and feet have all been implemented, with variable stiffness functionality, but variable damping has not yet been physically added.

#### A. Mechanical Design

BLUE is a planar biped, with powered hip, knee and ankle joints, each of which has variable stiffness and variable damping. There are two completely passive joints in each foot, and a powered torso joint, although this is only position controlled. In this work we present BLUE purely with variable stiffness, variable damping has been designed in but not yet implemented, and we will introduce this in a future paper. Similarly the torso joint and upper body will not feature here. The link lengths of BLUE are scaled from human anthropometric data [17], and are shown in Table II. The target weight of the robot is around 25kg, and without the torso or damping motors the current weight is around 18kg. The robot is supported laterally by a rotating boom arm, but is free to move in the sagittal plane.

Mimicking the design and function of the human foot, each of the feet are composed of three parts, with two sprung joints creating the longitudinal arch and toes, as shown in Fig. 7. The flexibility of the foot is important as it allows it to mould to the contours of the ground, increasing stability, as well as storing energy in ways a rigid foot could not [30] [31]. A compliant foot also gives a better roll-over shape than a rigid foot, supporting the robot more as it approaches toe-off. The design of the feet also allows for the easy implementation of a windlass mechanism, which stiffens the foot as the toes extend [32].

The main six joints of the robot are all based around the variable stiffness mechanism and motor braking variable damping as detailed before. When selecting drive motors, we looked at the likely torques and velocities which will be required, added a safety factor accounting for gearing efficiency losses, and selected an available motor which best meets the corresponding requirements. All six of the drive motors are 150W Maxon EC45 flat brushless DC motors, with a simple timing belt drive to the lead screws, allowing fast adjustment of stiffness. Joint angle requirements are taken from human movement data, with a mechanical stop preventing hyperextension of the knee joints and helping to bear load during the stance phase of walking.

The chassis of the robot is designed to be waterjet cut, in order to reduce the construction time. These parts are shown (not to scale) in Fig. 8(a), and the robot itself is shown in Fig. 8(b). Waterjet cut parts were machined in a standard manual mill to create any three dimensional features required.

#### B. Sensors and Electronics

Each variable impedance joint on the robot has two magnetic encoders to give the rotary positions of the intermediate arm and output link. Since we know the spring deflection and torque transfer function, it is also possible to calculate torque in the joints with this data. The drive motor electronics also include current sensing. The position of the spring carriage, and hence the stiffness setting, is measured by a simple linear...
TABLE III
SUMMARY OF THE SENSORS ON BLUE

<table>
<thead>
<tr>
<th>Sensor</th>
<th>Type</th>
<th>Implementation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Joint angle &amp; Intermediate arm angle</td>
<td>Rotary position</td>
<td>Magnetic encoders (Austria Microsystems A55040-ASSU)</td>
</tr>
<tr>
<td>Stiffness setting</td>
<td>Linear position</td>
<td>Linear potentiometer (Bourns PTA6043-2015DP-BI03)</td>
</tr>
<tr>
<td>Joint torque</td>
<td>Calculated</td>
<td>Virtual</td>
</tr>
<tr>
<td>Drive motor current</td>
<td>Analog readout</td>
<td>Built in to ESC</td>
</tr>
<tr>
<td>Ground reaction force</td>
<td>Force magnitude and distribution</td>
<td>Six Force Sensitive Resistors (Interlink FSR402)</td>
</tr>
<tr>
<td>Vestibular</td>
<td>Inertial measurement and tilt</td>
<td>3-axis accelerometer &amp; gyros (ADXL335, LY530AL, LPR530AL, HMC5843)</td>
</tr>
</tbody>
</table>

potentiometer. Six force sensitive resistors on each foot of the robot give information about ground reaction force on each of the three foot segments. Finally a 3-axis accelerometer and 3-axis gyro mounted on the torso of the robot give inertial measurement and tilt data. A summary of the sensors on the robot is given in table III.

The architecture of the electronics on the robot is shown in Fig. 9. A control board with ATMEL microcontroller (AT91SAM7x256) and Ethernet interface is present on each joint of BLUE. This communicates with a fitPC2i embedded computer running Arch Linux with a real time kernel. The fitPC runs the control program, sending target trajectories to the control boards of each joint. These boards interface with motor driver boards for each of the three motors on the joint, running PID loops for control of the drive and stiffness adjustment motors.

The control boards also read any relevant sensors, filter the data, and relay it back to the fitPC. For rotary sensor data from the magnetic encoders, a Synchronous Serial Interface (SSI) is used to obtain a digital readout from the encoder with 10 bit accuracy. This is then filtered through a moving average filter on the control board to give a very steady signal from these sensors. The other sensors - stiffness position, motor current, etc - are read through the ADC. All signals are sampled at 1kHz. An on board 8-port Ethernet switch is used to connect together the control boards and fitPC, and a wireless link is used to give high level commands to the fitPC from a remote computer.

V. EXPERIMENTS

In addition to building the hardware, we have developed a full physics dynamic simulation using the Choreonoid program [33] to effectively evaluate potential control strategies prior to testing them on the actual hardware. The results of implementing some basic controllers in both simulation and hardware will be discussed here. A video of these experiments is available online.

The CAD model of the robot was ported into Choreonoid with the appropriate mass and inertia properties, and the compliant joints were modelled with the appropriate spring transfer functions. Choreonoid allows for simulation in 2D (meaning the boom arm does not have to be modelled) and can simulate springs and dampers in the joints [34], including non-linear ones. The simulator runs faster than real time on a modern laptop.

Whilst the simulation results can not be expected to exactly match the performance on the hardware, they should allow for the evaluation and testing of potential controllers.

The hardware has been constructed as detailed above, complete with electronics capable of position or torque control, and turning off motors if motor current or joint position limits are breached. This gives a very fast fail-safe system which will prevent the hardware being damaged in the event that a control program does not perform as expected.

It was verified that the joints performed as expected, and particularly that the stiffness adjusters were capable of varying stiffness in a timely manner. Experiments show
that under no loading, the joint can vary from highest to lowest stiffness and back again within one second. This speed decreases as loading increases, mainly due to additional un-modelled frictional forces with the leadscrews. The physical hardware also experiences backlash on the joints, which is not modelled in the simulation.

The electronics and on-board Ethernet network perform very well, with no detected packet loss. Noise on the angle sensor readings is typically in the region of 0.3°.

A. Squatting

To provide a basic evaluation of the hardware without the need to worry about issues such as balance, we first conduct experiments with the robot performing continuous squats while the stiffness is changed. This demonstrates that the compliance of the robotic joints does change, and that this has physical results on the behaviour of the robot under a constant control scheme. For these tests, we perform high gain positional control on the intermediate arm, leaving the final link output position compliant through the variable stiffness mechanism.

Fig. 10 shows the commanded joint trajectories and link output positions for one of the knees of the robot, both in simulation and on the actual hardware. Similar graphs are observed for the ankles and hips. Both legs are given the same commands, and exhibit the same behaviour. We can observe that the effect of the compliance is noticeable even under these low velocity double-support movements. The hardware follows the same general trend as the simulation, but with some additional deflection due to backlash in the joint. Fig. 10(b) also shows the performance of a stiffness adjuster on the real hardware, and it can be observed that it is capable of rapidly altering the compliance of the joint.

B. Walking

Since the morphology of the robot is a scaled version of a human, and balance is simplified by the boom arm, we are able to use human walking data from motion capture in order to quickly produce a walking motion. This will not be the most efficient walk possible for the robot, since its mass distribution and joint dynamics are different from a human, but it is a good starting point. First we replay the joint data from human walking with a high stiffness setting, to validate that it does indeed produce stable walking behaviour on the robot. Fig. 11 shows scenes from the walking sequence in simulation and on the physical robot.

When a trajectory was successful on the simulator, it was played back on the hardware. Fig. 12 shows a walking motion on the ankle and knee joints of one leg. In the absence of a torso to aid balance, it was necessary to add a small counterweight to the boom arm, relieving approximately a third of the weight from the robot. The dynamic loading of the joints can be seen in their deflection from equilibrium, as for these experiments only the equilibrium position is being controlled.

VI. CONCLUSION

Variable impedance technology can be extremely beneficial to bipedal robots, in helping them to be inherently robust to disturbances, and potentially more efficient in their...
locomotion. We evaluated the wide spectrum of literature of variable impedance actuation in order to select appropriate methods for variable stiffness (tunable springs) and variable damping (motor braking) which seem most suitable for providing the required torque and stiffness required in bipedal locomotion, but which, importantly, can maintain joints at a high stiffness without requiring the expenditure of energy.

We looked at the dynamics of human walking to design a robot which should be capable of mimicking such motion, and have shown both in simulation and on the actual hardware, that walking can be achieved. Furthermore we have shown that the variable stiffness mechanism in BLUE is capable of changing the stiffness of its joints to noticeably affect its dynamics. We have also designed a robust, compact, set of electronics and sensors to control the robot. Future work will concentrate on the performance of the variable damping, and on control strategies for best utilising the variable dynamics of the robot.

REFERENCES